

## SOLUTION

**Que:71**

Given that DE and FG are both parallel to B.

⇒ DE is parallel to FG.

∴  $\Delta ADE \sim \Delta AGF$

Since the area of  $\Delta ADE$  is equal to the area of the quadrilateral DEGF, the area of  $\Delta AFG$  is twice the area of the  $\Delta ADE$ .

$$\frac{\text{Area of } \Delta ADE}{\text{Area of } \Delta AFG} = \left(\frac{AD}{AF}\right)^2 = \left(\frac{AE}{AG}\right)^2 = \left(\frac{DE}{FG}\right)^2$$

$$\therefore \left(\frac{DE}{FG}\right)^2 = \frac{1}{2}$$

$$\Rightarrow \frac{DE}{FG} = \frac{1}{\sqrt{2}}$$

**Que:72**

Given equation  $31x + 13y = 75$ .

(A) (2, 1) satisfies the given equation  $31(2) + 13(1) = 75$ .

Any pair (x, y) satisfying the equation can be expressed in the form  $(2-13K, 31K+1)$  where k is an integer.

∴ When  $K=1$   $(2 - 13(1), 31+1) = (-11, 32)$

When  $K=2$   $(2 - 13(2), 31+2) = (-24, 63)$

$K=3$   $(2 - 13(3), 31+3) = (-37, 94)$

∴ Option (D) does not satisfy the given equation.

**Que:73**

It is sufficient to compare the ratio  $\frac{20.7}{32.8}$  (i.e., mango) with the ratio  $\frac{27.4}{6.9}$ ,  $\frac{19.4}{11.8}$ ,  $\frac{5.8}{14.3}$ ,  $\frac{4.6}{6.1}$ ,  $\frac{18.7}{24.7}$  and

$\frac{3.4}{3.4}$

By observation, only  $\frac{5.8}{14.3}$  (i.e., Apples) is less than  $\frac{20.7}{32.8}$ . Hence only one variety of fruit.

**Que:74**

Export price per tonne for walnuts is proportional  $\frac{27.4}{6.9}$  which is the highest ratio.

Statement A is true as Walnuts has the highest ratio of value to quality.

Statement B is true as  $\frac{20.7}{32.8} < \frac{18.7}{24.7}$ .

Statement C is true as  $\frac{3.4\% \text{ of } x}{3.4\% \text{ of } y} = \frac{x}{y}$ .

Statement D is true as  $\frac{19.4\%}{11.8\%} < 2 \left(\frac{3.4}{3.4}\right)$ .

**Que:75**

Let the total production of all the fresh fruits be 100.

⇒ Exports of fresh fruits = 30

From the 1<sup>st</sup> pie-chart, exports of mango = 32.8% of exports of all fresh fruits = 32.8% of 30 which is 20% of the production of mangoes.

$$\therefore 32.8\% \text{ of } 30 = 20\% P_M \Rightarrow P_M = \frac{32.8 \times 30}{20} = 49.2$$

Out of the total production of 100, share of mangoes = 49.2 or 49.2%.

**Que:76**

If the money is equal in dollars terms, then it will be so even in rupee terms. A Robert got 24 + 8 = 32 rupees and now all of three have equal amount.

Total amount = 32\*3 = 96 rupees

Total amount = (12D+5E) + (8D+4E) = 20D+9E

$$\therefore 20D+9E=96$$

Also after giving 8 rupees to Robert, Nelson is left with 32 rupees.

$$\Rightarrow 8D + 4E - 8 = 32$$

$$\Rightarrow 2D + E = 10 \rightarrow (2)$$

$$(2) * 10 - (1) \text{ gives } E = 4.$$

**Que:77**

Let Nelcy and Mike together can complete the work in n days.

⇒ Nelcy takes (n+12) days

⇒ Mike takes (n+27) days

$$\therefore \frac{1}{(n+12)} + \frac{1}{(n+27)} = \frac{1}{n}$$

$$\Rightarrow n[(n+12) + (n+27)] = (n+12)(n+27)$$

$$\Rightarrow 2n^2 + 39n = n^2 + 39n + (27)(12)$$

$$\Rightarrow n^2 = (27)(12) = 324$$

$$\Rightarrow n = 18$$

But Nelcy and Mike worked for only 15 days.

⇒ They completed  $\frac{15}{18} = \frac{5}{6}$  th of the work.

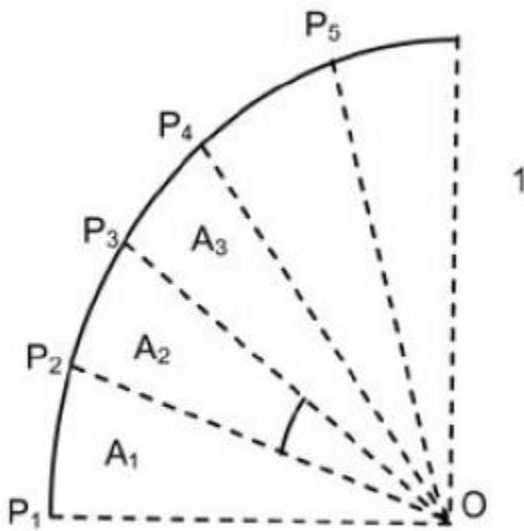
⇒ James completed  $\frac{1}{6}$  th of the work.

∴ James share =  $\frac{1}{6}(3000) = \text{Rs. } 500$

**Que:78**

Observe that  $(-1)^{2i} = 1$ , for all values of  $i$ . Hence  $OP_1 = OP_2 = OP_3 \dots = OP_n = 1$  unit.

Consider the section of polygon as shown.



As we choose large value of 'n' we make the figure close to a circle of radius 1 unit.

Hence for large values of 'n', the area of polygon will be closed to  $\pi(1)^2 = \pi$  sq.units

**Que:79**

$2x + 5$  is an increasing function and  $14 - x$  is a decreasing function.

Min  $[\max(2x+5, 14 - x)]$  occurs when the increasing and decreasing functions become equal.

$$\therefore 2x + 5 = 14 - x$$

$$\Rightarrow 3x = 9$$

$$\Rightarrow X = 3$$

Substituting  $x = 3$  in any of the functions =  $2(3) + 5 = 11$

**Que:80**

Let AD be perpendicular to BC, the largest side.

Area of triangle ABC = 152

$$\Rightarrow \frac{1}{2}(38)(AD) = 152$$

$$\Rightarrow AD = 8$$

AS ABCD is right angled triangle,  $AB^2 = AD^2 + BD^2$

$$\Rightarrow 100 = 64 + BD^2$$

$$\Rightarrow BD = 6$$

$$\Rightarrow CD = 32$$

$\Rightarrow$  Also  $\Delta ADC$  is aright angled triangle.

$$\Rightarrow AC^2 = (32)^2 + (8)^2$$

$$\Rightarrow AC = \sqrt{1088} = 8\sqrt{17}$$

**Que:81**

Let the amounts with Anna, Ben and Clark be Rs. A, Rs. B and Rs. C respectively.

$$a + b + c = 100$$

$$4(a-13) = b+13$$

$$3(c-7) = b+7$$

Solving these equations, we get  $a = \text{Rs. } 28$ ,  $b = \text{Rs. } 47$ , and  $c = \text{Rs. } 25$

Let the sum that Ben need to give to Clark be Rs. X such that they have the same amount.

$$47-X = 25+X \text{ or, } X=11.$$

**Que:82**

Model	Revenue from Sales	Revenue from Service
<b>Brio</b>	6.4% of 20 = 1.28	30.5% of 12 = 3.66
<b>Jazz</b>	10.15% of 20 = 2.03	24% of 12 = 2.88
<b>Civic</b>	9% of 20 = 1.8	18.2% of 12 = 2.184
<b>City</b>	18% of 20 = 3.6	15% of 12 = 1.8
<b>Accord</b>	30% of 20 = 6	6.1% of 12 = 0.732
<b>CR-V</b>	26.45% of 20 = 5.29	6.2% of 12 = 0.7444

Combined revenue, Rs. 6,732 Cr, is highest for Accord.

**Que:83**

$$\text{Volume of cars sold of Brio} = \frac{6.4}{100} * \frac{20}{4}$$

$$\text{Of Jazz} = \frac{10.15}{100} * \frac{20}{5.8}$$

$$\text{Of Civic} = \frac{9}{100} * \frac{20}{7.2}$$

$$\text{Of City} = \frac{18}{100} * \frac{20}{12}$$

$$\text{Of Accord} = \frac{30}{100} * \frac{20}{20}$$

$$\text{Of CR-V} = \frac{26.45}{100} * \frac{20}{23}$$

It can be seen that the least number of cars sold is of CR-V, which is equal to 23.

**Que:84**

Say the no. of cars sold of the six brands is  $6k_1, 7k_1, 5k_1, 6k_1, 6k_1, 5k_1$  respectively.

Say the no. of cars serviced of the six brands is  $6k_2, 7k_2, 5k_2, 6k_2, 6k_2, 5k_2$  respectively.

Sum of revenue per car from sales and from service.

$$= \frac{6.4\%}{6k_1} + \frac{30.5\% \text{ of } 12}{6k_2}$$

Revenue obtained per car of Jazz

$$= \frac{10.15\% \text{ of } 20}{7k_1} + \frac{24\% \text{ of } 12}{7k_2}$$

Similarly the expressions for other cars can be written. Unless some relation between  $k_1$  and  $k_2$  is known, the expressions cannot be determined.

$\therefore$  It cannot be determined.

**Que:85**

Say 3 stations are chosen from the 38 intermediate stations between Gudivada and Yaddanapudi such that they are not consecutive. There are 35 remaining stations, which will have 36 gaps.

$\Rightarrow$  The 3 stations should have been chosen from the 36 gaps.

$\Rightarrow \therefore$  No. of ways =  ${}^{36}C_3 = 7140$ .

**Que:86**

If the root are real, then discriminate  $\geq 0$

$$\Rightarrow p^2 - 4 * 12 \geq 0$$

$$\Rightarrow p^2 \geq 48$$

$$\Rightarrow |p| \geq \sqrt{48}$$

$$\Rightarrow |p| \geq 4\sqrt{3}$$

But p is the sum of the roots  $\alpha_1$  &  $\alpha_2$

$$\Rightarrow |\alpha_1 + \alpha_2| \geq 4\sqrt{3}$$

**Que:87**

The equation of the passing through (3,5) and (2,2) is  $y - 2 = \frac{5-2}{3-2} (x - 2)$  or  $3x - y = 4$ .

Now since the point  $(a+1, 3a - 1)$  satisfies the above equation i.e.  $3(a + 1) - (3a - 1) = 4$ . So any real value of 'a' will satisfy the above equation.

**Que:88**

$$f(1 + 1) = f(2) = f(1) \quad f(1) = f^2(1) = 16^2$$

$$f(3) = f(2)f(1) = 16^2 * 16 = 16^3$$

$$f(4) = 16^4$$

.

.

.

.

$$f(x) = 16^x.$$

$$\therefore f\left(\frac{3}{4}\right) = 16^{\frac{3}{4}} = 8$$

**Que:89**

Using statement 1 alone, the possible number of students in the class can be 19, 18, 17... To 5. So it is not sufficient alone

Using statement 2 alone, the possible number of students in the class are 13, 14, 15,...Again not sufficient alone.

Even if we combine both, we get multiple values possible. Hence, no unique answer.

**Que:90**

Using Statement 1 alone, B & C together earns \$350. Individual salary of them can't be unique and we can't conclude the highest value

Using statement 2 alone, A & C earns \$250 combined. Now the highest has to be 250\$ which is drawn by B as A & C both earns less than 250\$.

So, statement 2 alone is sufficient.

**Que:91**

Using statement 1 alone, the sixth men height is 5 feet, which alone is not sufficient to say anything about the height of 5th men in the queue ( From front end of the line)

Using statement 2 alone,

$$\text{Height of } 6^{\text{th}} \text{ man} = 4 * \text{Height of } 5^{\text{th}} \text{ man} \text{ --- (1)}$$

Height of 7<sup>th</sup> man = 8\* Height of 6th man — (2)

Even after solving both equations, we can get a absolute value as both equation give only relation and no absolute value,

Combining both statements, we can get a unique.

**Que:92**

Using statement 1 alone, the total area of the square can be derived. The shaded portion will be  $\frac{1}{4}$  of the total area. Hence, alone 1 is sufficient.

Using statement 2 alone, the diagonal length is given. Diagonal of square is always square root of 2 times the length of square. We can hence derive the area and the shaded portion will be  $\frac{1}{4}$ th of the total and a unique answer can be derived. Hence, alone 2 is also sufficient.

**Que:93**

Using statement 1 alone,  $R > Q$ . We can't say anything about  $P > Q$ . Hence, 1 alone is not sufficient.

Using statement 2 alone,  $R > P$ . Again we can't say anything about  $P > Q$ . Hence, statement 2 alone is not sufficient.

Combining both statements,  $R > P$  and  $R > Q$ . But we cannot get a unique relationship between P and Q.

Both are not sufficient.

**Que:94**

Age of Thomas can be 8, 27 or 64.

Using statement 1 alone, the only age possible is 27. Hence, 1 alone is sufficient.

Using statement 2 alone, the only possible age is 64. Hence, 2 alone is sufficient.

**Que:95**

Average number of applications received

$$= \frac{\text{Total Number of applications received}}{4}$$

The % change in the average number if applications received per university is same as that for total number of applications. In 2007, total number of applications =  $18926 + 16723 + 18428 + 19201 = 73, 276$ .

In 2009, total number of applications received = 85701. % Increase =  $\frac{85701 - 73728}{73728} * 100 = 16.95\%$ .

<b>Que:96</b>	
<p>For University R, % increase in applications from 2006 to 2007 = <math>\frac{184-157}{157} * 100 = 17\%</math></p> <p>Similarly,</p> <p>2007 to 2008 is 12%, 2008 to 2009 is 4% and 2009 to 2010 is 9%. Least % increase occurred in 2009.</p>	
<b>Que:97</b>	
<p><math>41n = (40 + 1)^n</math>. This means x = number of factors of 40 which is equal to 8.</p>	
<b>Que:98</b>	
<p>Go by options, option 1 is eliminated as she cannot offer all the flowers.</p> <p>Take option (4) Let flower be n. After putting into the water = 2n. <math>\frac{1}{4}^{\text{th}}</math> of 2n offered to the first place of worship = <math>\frac{2n}{4}</math>. Remaining <math>\frac{3n}{2}</math>. After putting <math>\frac{3n}{2}</math> flower into water they become 3n flowers, <math>\frac{1}{4}^{\text{th}}</math> of 3n offered to the second place of worship. Remaining = <math>\frac{9n}{4}</math>. Hence required ratio = <math>\frac{2n}{4} : \frac{9n}{4} = 2 : 9</math>.</p>	
<b>Que:99</b>	
<p>p can be 3 or 7, but unit digit of <math>(p + 1)^2 = 4</math>. <math>p = 7</math>. Hence unit digit of <math>(7 + 2)^2 = 1</math>.</p>	
<b>Que:100</b>	
<p>As the given equation has imaginary root, they will be conjugate to each other. In this case, both roots will be common or a: b: c = 1: 2: 3.</p>	
<b>Que:101</b>	
<p><math>A_{20} = 1 + 3 + 5 + \dots</math> 20 terms = <math>\frac{20}{2} [2 + 19 * 2] = 400</math>. So the first term of <math>A_{21}</math> is 401.</p>	
<b>Que:102</b>	
<p>In order to form a pair, the first female will (n - 1) trials, the second (n-2) trials and so the total number = <math>n(n-1)/2</math>.</p>	
<b>Que:103</b>	
<p>In the given progression, first term = 19, common difference = <math>18.5 - 19 = -4/5</math>. Since the common difference is negative, each successive term is decreasing and here will be negative terms. Let nth term be the first negative term. Then nth term <math>&lt; 0 \Rightarrow an &lt; 0 = a_1 + (n-1)d &lt; 0</math>. Solving for n we get n=25.</p> <p>Here, 25th term is the first negative term and the first 24 terms will be non-negative. The sum will</p>	



be maximum if no negative terms are taken. So, summing up to the 24 terms will be considered.  
 Maximum sum =  $S_{24} = 24/2 * [2(19) + 24 - 1] (-4/5) = 235.5$ .

**Que:104**

The given term is constant and there cannot be minimum and maximum value of a constant term.

**Que:105**

For all values of n, we get  $f(n) = 1/n$ . So the required answer =  $1 + 2 + 3 + \dots + 9 = 45$ .

**Que:106**

Using statement 1 alone, Since  $m - n$  is a multiple of 22,  $m - n$  is multiple of 11 and 2 ( $11 * 2 = 22$ ). If both  $m$  and  $n$  are multiples of 11, then their sum is also multiple of 11. However, if  $m$  and  $y$  are not individually divisible by 11, it is possible that  $m - n$  is a multiple of 22 while  $m + n$  is not a multiple of 11. Hence, alone 1 is not sufficient.

Using statement 2 alone, possible values are 11, 22, ..., 99. Since each of the values is a multiple of 11,  $m$  must be a multiple of 11. Now if both  $m$  and  $n$  are multiples of 11,  $(m + n)$  and  $(m - n)$  will be a multiple of 11. Hence, statement 2 alone is sufficient.

**Que:107**

$|2x - 19| < 7$ , implies that  $-7 < 2x - 19 < 7$ , implies that  $x > 13$  or  $x < 13$ . Hence statement 1 alone is not sufficient.

Statement 2 implies that  $x = 0$  or  $x = 4$ . Hence, not sufficient. Even after combining both the statements, unique solution cannot be obtained.

**Que:108**

Using statement 1 alone,  $3x + 5y = 11$  can't derive unique relation between  $x$  and  $y$  (if  $x = 2$ ,  $y = 1 \Rightarrow x > y$  & if  $x = (-2)$ ,  $y = 7 \Rightarrow x < y$ ). Hence 1 alone is not sufficient.

The odd power of  $x$  is greater than the odd power of  $y$ . It implies that  $x$  is greater than  $y$  and hence sufficient.

**Que:109**

For any  $n$ ,  $199^{2n}$  has last digit as 1. But the last digit of  $144^{2n}$  is 4 for odd values of  $n$  and 6 for even values of  $n$ . Therefore, last digit of the expression is either 5 or 7.

**Que:110**

Relative speed of A and B will be 20 m/min to cover the track of 960m. It will take 48 min.

**Que:111**

Let's assume the total amount of work = 32 units.

So A and B does 2 units per day. A does 1 unit per day so B does 1 unit per day. Hence, 32 units of work will be completed in 32 days.